Mathematics for Computer Science, CM0167,
Example class, Week 9,
Dr David Marshall

1. A student either walks to university or goes by train. If one day he goes to university by train, then the probability that he goes by train the next day is $\frac{7}{10}$. If one day he walks to university then the probability the he goes by train the next day is $\frac{2}{5}$.
Given that he walks to university on a Tuesday, draw a probability tree diagram and hence find the probability that he will go to university by train on Thursday of that week.
2. Let $A$ and $B$ be two events such that $P(A)=\frac{1}{4}$ and $P(B)=\frac{2}{5}$ and $P(A \cap B)=\frac{1}{5}$.
(a) Calculate $P(A \mid B)$ and $P\left(A \mid B^{c}\right)$.
(b) Determine $P(A \mid B) P(B)+P\left(A \mid B^{c}\right) P\left(B^{c}\right)$ without any calculations. (Hint: Theorem of total probability)
3. Simple Classification Example.Three aircraft are known to fly out of an airport with the respective probabilities: Airbus A320, 0.5, Boeing 747, 0.4 and a Antonov AN124-100 Cargo plane, 0.1. The aircraft are know to take off with the following probabilities speeds: Airbus A320 speed greater than $300 \mathrm{mph}, 0.7$, Airbus A320 speed less than $300 \mathrm{mph}, 0.3$; Boeing 747 speed greater than $300 \mathrm{mph}, 0.6$, Boeing 747 speed less than 300 mph , 0.4; Antonov AN124-100 speed greater than $300 \mathrm{mph}, 0.1$, speed less than $300 \mathrm{mph}, 0.9$.
Given that a radar at the airports detects an aircraft with a speed of 350 mph what is probability it is an Airbus A320, Boeing 747 or a Antonov AN124-100?
4. (a) An unfair coin is tossed 20 times. The probability that it lands on Heads is $\frac{1}{3}$. If $X$ is defined as the number of tosses that result in Heads, what is the expectation of $X$.
(b) The same coin as above is tossed 20 times again. Jim gets 2 pounds if the coin results in Heads and loses 1 pound if it results in Tails. What is his expected net profit or net loss.
5. If you play a roulette game you can choose between the numbers $0,1, \ldots, 36$. If you bet on the right number you get your money back plus 5 times the money you have bet. What is your expected net profit or net loss?
